

## The Measurement of Elasticities

### General meaning of elasticity of demand:

From the theory of demand we know that the **amount of a commodity** purchased per unit of time is a function of or **depends on the price of the** commodity, money incomes, the price of other (related) commodities, tastes, and the number of buyers of the commodity in the market. A change in any of the above factors will cause a change in the amount of the commodity purchased per unit of time. The elasticity of demand measures the relative responsiveness in the

amount purchased per unit of time to a change in any one of the above factors, while keeping the others constant. **Price Elasticity Of Demand**

The coefficient of *price elasticity of demand* ( $e$ ) measures the percentage change in the quantity of a commodity demanded per unit of time resulting from a given percentage change in the price of the commodity. Since price and quantity are inversely related, the coefficient of price elasticity of demand is a negative number. In order to avoid dealing with negative values, a minus sign is often introduced into the formula for  $e$ . Letting  $\Delta Q$  represent the change in the quantity demanded of a commodity resulting from a given change in its price ( $\Delta P$ ), we have

$$\frac{\Delta Q/Q}{\Delta P/P}$$

$$= \frac{\Delta Q}{\Delta P} \cdot \frac{P}{Q}$$

$$= \frac{\Delta Q}{Q} \cdot \frac{P}{\Delta P}$$

Demand is said to be *elastic* if  $e > 1$ , *inelastic* if  $e < 1$  and *unitary elastic* if  $e = 1$ . **EXAMPLE 1.** Given the market demand schedule in Table 1.1 and market demand curve in Fig. 1-1, we can find  $e$  for a movement from point B to point D and from *D to B*, as follows:

$P: (\$)$

Table 1.1 Point  $PX(\$)$   $Q_x$

A 8 0 B 7 1000

6 2000

3000 F 4 4000 G 3 5000

6000 L 1 7000 M 0 8000

1000

3000 5000 7000

Fig. 1-1

From B to D,

$$e = -\frac{P_B - P_D}{Q_B - Q_D} = -\frac{2000 - 7000}{11000 - 7000} = 1.67$$

$$P_D - P_B = 2000 - 7000 = -5000$$

From D to B,

$$e = -\frac{P_D - P_B}{Q_D - Q_B} = -\frac{-5000}{-3000} = 1.67$$

We can avoid getting different results by using the average of the two prices  $[(P_B + P_D)/2]$  and the average of the two quantities  $[(Q_B + Q_D)/2]$  instead of either  $P_B$  and  $Q_B$  or  $P_D$  and  $Q_D$  in the formula to find  $e$ . Thus,

$$e = -\frac{P_B + P_D}{Q_B + Q_D} \Delta Q = -\frac{P_B + P_D}{Q_B + Q_D} \Delta Q$$

Applying this modified formula to find  $e$  either for a movement from B to D or for a movement from D to B we get

$$e = -\frac{2000 + 7000}{11000 + 7000} \Delta Q = -\frac{9000}{18000} \Delta Q = -0.5 \Delta Q$$

**This is the equivalent of finding  $e$  at the point midway between B and D (ie, at point C).**

Example-2. Given the market demand schedule in Table 1.2 and the market

demand curve in Fig. 1-2, we can find  $e$  for a movement from point C to point F, from F to C and midway between C and F, as follows: Table 1.2

P.(\$)

Point P (\$) Qx

7 500 6 750

5 1250 D 4 2000

3 3250 G 2 4750 H 1 8000

2000 4000 8000

Fig. 1-2

From C to F,

$$e = -\frac{P_C - P_F}{Q_C - Q_F} = -\frac{3250 - 7000}{4750 - 8000} = 20.92$$

From F to C

$$e = -\frac{P_F - P_C}{Q_F - Q_C} = -\frac{7000 - 3250}{8000 - 4750} = 20.92$$

At the point midway between C and F (point D on the dashed chord),

$$e = -\frac{P_C + P_F}{Q_C + Q_F} \Delta Q = -\frac{3250 + 7000}{4750 + 8000} \Delta Q = -\frac{10250}{12750} \Delta Q = -0.808 \Delta Q$$

## POINT ELASTICITY

Point elasticity of demand: The coefficient of price elasticity of demand at a particular point on a demand curve.

EXAMPLE 3. We can find the elasticity of demand curve in Example 1 at point C geometrically as follows. (For easy reference, Fig. 1-1, with some modifications, is repeated here as Fig. 1-3). Since we want to measure elasticity at point C, we have

only a single price and a single quantity. Expressing each of the formula for  $e$  in terms of distances, we get:

$P, (\$)$

$$e = \frac{\Delta Q}{Q} \frac{P}{\Delta P}$$

$$e = - \frac{AP}{P} \frac{P}{CQ}$$

$$= - \frac{NM}{ON} \frac{NC}{ON} \frac{ON}{NM} \frac{6000}{2000}$$

$$= - \frac{4000}{6000} \frac{6000}{2000}$$

$$= -3$$

2000

8000

4000 6000 Fig. 1-3

## INCOME ELASTICITY OF DEMAND

The coefficient of income elasticity of demand ( $e_m$ ) measures the percentage change in the amount of a commodity purchased per unit of time ( $\Delta Q/Q$ ) resulting from a given percentage change in a consumer's income ( $\Delta M/M$ ). Thus

$$e_m = \frac{\Delta Q/Q}{\Delta M/M} = \frac{\Delta Q}{Q} \frac{M}{\Delta M}$$

When  $e_m$  is negative, the good is inferior. If  $e_m$  is positive, the good is normal. A normal good is usually a *luxury* if its  $e_m > 1$ , otherwise it is a *necessity*. Depending on the level of the consumer's income,  $e_m$  for a good is likely to vary considerably. Thus a good may be a luxury at "low" levels of income, a necessity at "intermediate" levels of income and an inferior good at "high" levels of income.

EXAMPLE 4. Columns (1) and (2) of Table 1.3 show the quantity of commodity X that an individual would purchase per year at various income levels. Column (5) gives

the coefficient of income elasticity of demand of this individual for commodity X *between* the various successive levels of available income. Column (6) indicates the range of income over which commodity X is a luxury, a necessity or an inferior good.

Table 13

Income (M) (S/year) (2)	(3) Quantity of Change (units/year) in Qi	Percent Change in M (6) Type of Good
8,000	—100	
12,000	10	
16,000	—1.50	luxury
20,000	15	
25,000	50%	
30,000	33.33	
35,000	—16	
40,000	16,000	luxury
45,000	—20	
50,000	254	
55,000	—	necessity
60,000	18	
65,000	14	

20—  
 -0.56%  
 necessity  
 24,000  
 20  
 -0.30  
 -inferior  
 28,000  
 19  
 — -5.26 —  
 1429 —  
 0.37—  
**inferior**  
 32,000  
 18

### CROSS ELASTICITY OF DEMAND

The coefficient of cross *elasticity of demand* of commodity X with respect to commodity Y ( $e_{xy}$ ) measures the percentage change in the amount of X purchased per unit of time ( $\Delta Q_x / Q_x$ ) resulting from a given percentage change in the price of Y ( $\Delta P_y / P_y$ ). Thus

$$e_{xy} = \frac{\Delta Q_x / Q_x}{\Delta P_y / P_y}$$

If X and Y are substitutes,  $e_{xy}$  is positive. On the other hand, if X and Y are complements,  $e_{xy}$  is negative. When commodities are nonrelated (i.e., when they are independent of each other),  $e_{xy} = 0$ .

**SAMPLE 5.** To find the cross elasticity of **demand between tea (X) and conce (Y)** and between tea (X) and lemons (Z) for the data in the **next table, we proceed** as follows.

Table 1.4 (a)

Before Price	Quantity (cents/cup) (units/month)
50	20
40	40
Commodity Coffee (Y)	

After Price Quantity (cents/unit) (units/month)

60 T 30 20 T 50  
Tea (X)

Table 1.4 (b)

Before  
After

Commodity Lemon (Z) Tea (X)

Price (cents/unit) - 10

20

Quantity (units/month)

20 T 40

Price (cents/unit)

20 T 20

Quantity (units/month) T 15

35

$$\frac{-4Q_x \cdot P_y}{P_x} = \frac{(+1040)}{20} = +0.5$$

$$e_{xy} = \frac{\Delta P_y}{P_y} \cdot \frac{Q_x}{1}$$

one tra le mie

$$9 - 0.125$$

Since  $e_{xy}$  is positive, tea and coffee are substitutes. Since  $e_{xz}$  is negative, tea and lemons are complements.